

# Preparing to succeed in A-level Maths College Preparation Work

Welcome to college and to the Mathematics Department.

You will now have a long break from school and may well find that you get rather rusty at some of the maths skills which you spent so long learning at school.

This booklet contains some of those key ideas from GCSE which will help you to make a good start on the A-level course. Please work through this booklet over the next few weeks to keep your skills up to speed.

The step up from GCSE to A-Level is a big leap. There are additional resources available to practice essential maths skills on the "summer homework" section of our college website <u>https://www.scg.ac.uk/pre-enrol</u> – please do these for extra practice.

Read through the examples for each topic and have a go at the questions in each bold section. Please make a good attempt at every question - we'd rather it was wrong than blank as it helps us to see where you may need some help! It's fine to look things up in your old books, or look at websites like BBC GCSE Bitesize to get some help if you need it.

Please set out all your working carefully and <u>try not to use a calculator</u> for any of these questions - algebraic skills are tested in the exams.

#### Preparing for lessons in September – please bring:

- A4 file paper (lined not squared is preferable)
- A ring binder folder with some file dividers
- Pens and pencils
- Highlighter pens
- This booklet to hand in!



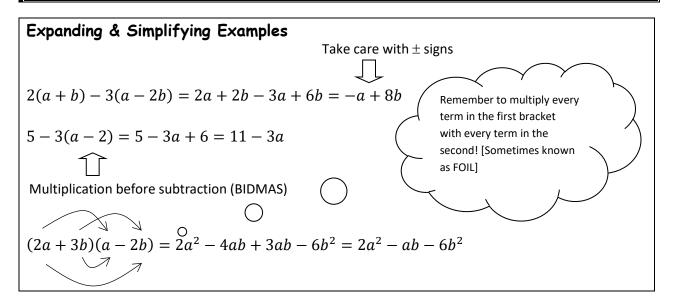


The following words or phrases are commonly used in A-level maths – how many do you recognise? Please jot down a brief definition of each term – look them up if you're not sure...

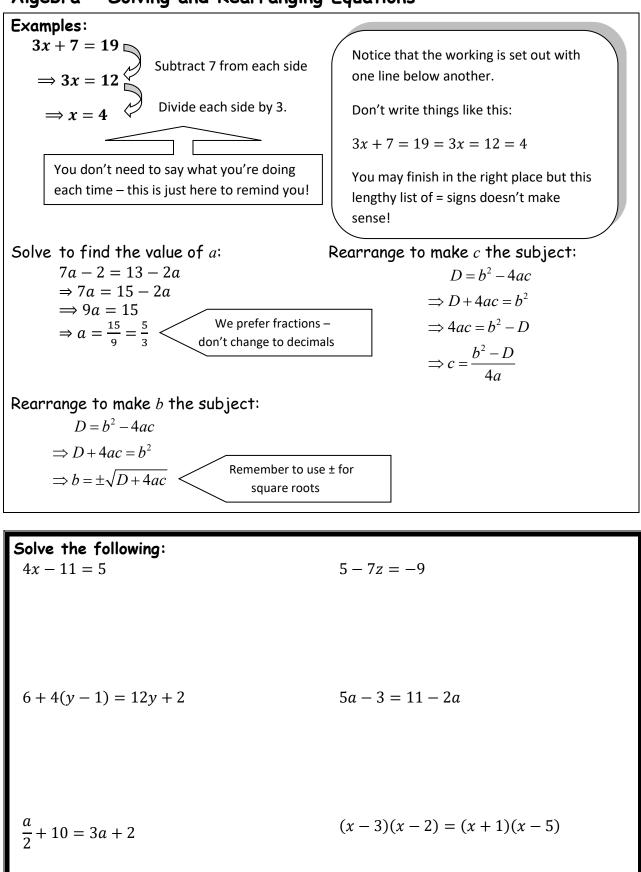
	Definition
Integer	
Rational	
number	
Numerator	
Denominator	
Irrational number	
Reciprocal	
Surd	
Polynomial	
Quadratic	
Linear	
Coefficient	
Gradient	
Parallel	
Perpendicular	
Tangent	
The Subject of an equation	

Algebra – substituting values, expanding brackets & collecting terms

Substitution: If a = 2, b = -3 and c = 5 find the values of the following expressions:  $a^{2} + b^{2} =$ 3ab - 2bc =(2a - b)(b + c) = $2c^{2} - abc =$ 



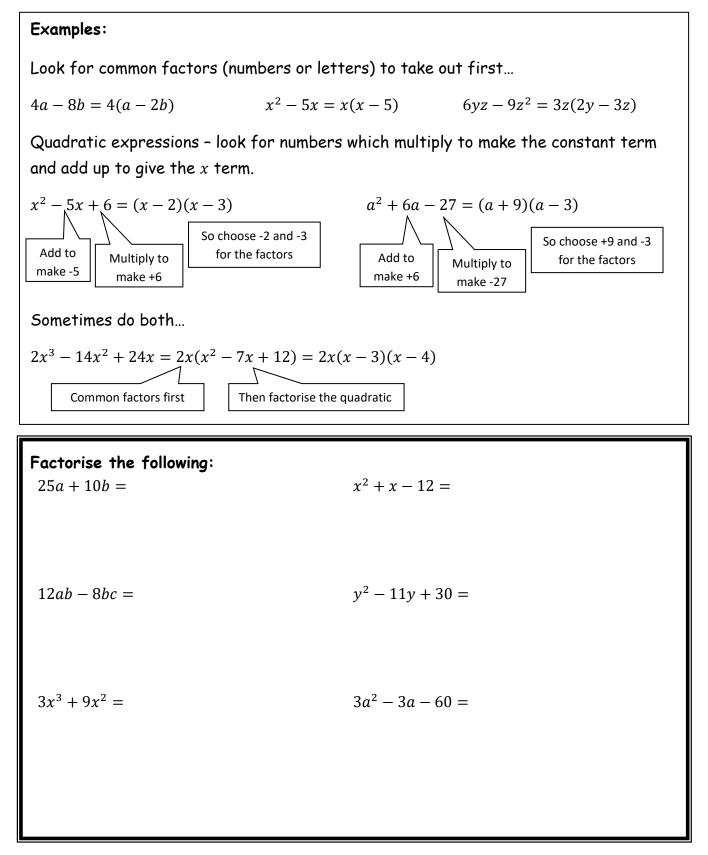
Try the following: 3(a + 10) + 2(a - 3) = 12 - 7(x + 3) = (3x - y)(2x + 4y) = (2a - 3)(2a + 3) =(2x - 3)(x - 2) =



## Algebra - Solving and Rearranging Equations

Rearrange the following formulae: Make y the subject: 3x - y = 53y - 6x - 4 = 0Make r the subject:  $S = 4\pi r^2$ x = m - 3rMake *a* the subject:  $b = \frac{a^2}{2}$  $b = \frac{\sqrt{a+2}}{c}$ 

## Algebra - Factorising



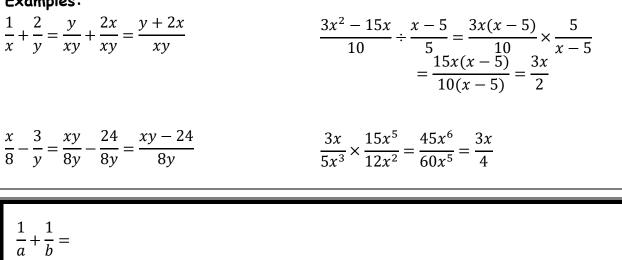
## **Algebraic Fractions**

### Rules :

You can add or subtract fractions if they have <u>a common denominator</u>. Multiply by multiplying the numerators and multiplying the denominators. Dividing by a fraction is the same as multiplying by the reciprocal (turn it over!) Don't forget to cancel fractions into their simplest possible form even when algebraic.

If unsure try a numerical version and use the same method for algebra.

#### Examples:



$$a \quad b$$

$$\frac{3}{x^2} - \frac{1}{x} =$$

$$\frac{2}{x^3} \times \frac{x^2}{8} =$$
(Remember to simplify!)
$$\frac{1}{x} \div \frac{1}{y} =$$

$$\frac{a}{b} - \frac{a}{b+1} =$$

$$\frac{1}{x+1} + \frac{1}{x-1} =$$

$$\frac{x-4}{x+3} \div \frac{2x-8}{3} =$$

$$\frac{3a^2 - 3a - 60}{a^2 - 2a - 24} =$$

#### Solving Quadratics

You can solve quadratic equations in the form  $ax^2 + bx + c = 0$  by Factorising .  $6x^2 - 11x - 10 = 0$  $\Rightarrow (3x+2)(2x-5) = 0$  $\Rightarrow$  3x+2=0 or 2x-5=0  $\therefore x = -\frac{2}{3} \text{ or } x = \frac{5}{2}$ Completing the square  $x^{2} + 12x + 3 = 0$  $\Rightarrow (x+6)^2 - 36 + 3 = 0$  $\Rightarrow (x+6)^2 - 33 = 0$  $\Rightarrow (x+6)^2 = 33$  $\Rightarrow x + 6 = \pm \sqrt{33}$  $\Rightarrow x = -6 \pm \sqrt{33}$  $\therefore$   $x = -6 - \sqrt{33}$  or  $x = -6 + \sqrt{33}$  [exact solutions]  $\therefore x = -0.255 \text{ or } x = -11.7 \text{ [to 3 s.f.]}$ 

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Remember to simplify all of these

Using the Quadratic Formula

•

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$5x^{2} + 2x - 3 = 3x^{2} - 5x + 7$$
  

$$\Rightarrow 2x^{2} + 7x - 10 = 0$$
  

$$[a = 2, b = 7, c = -10]$$
  

$$\Rightarrow x = \frac{-7 \pm \sqrt{7^{2} - 4(2)(-10)}}{2(2)}$$
  

$$\Rightarrow x = \frac{-7 \pm \sqrt{129}}{4} \text{ [exact solutions]}$$

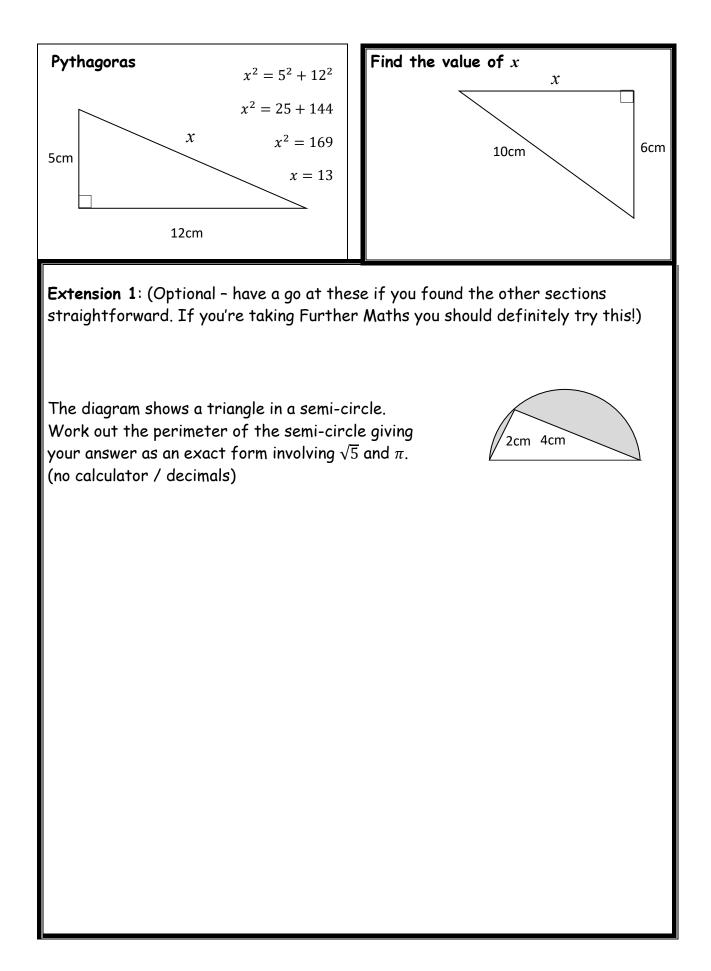
Solve by factorising (solve means find the values of x)  $4x^2 + 25x - 21 = 0$ 

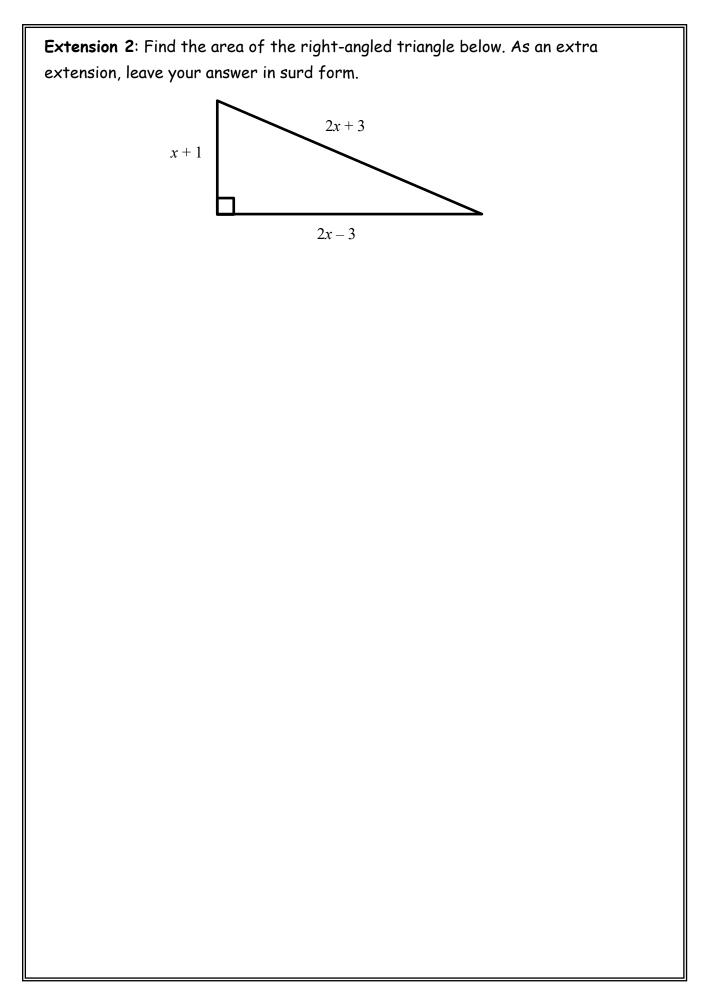
Solve by completing the square

$$x^2 + 8x - 1 = 0$$

Solve By Using The Quadratic Formula  $3x^2 - 5x - 2 = 0$ 

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